

# Lab 2

Dr. Donald Davendra  
CS471 - Optimization

October 12, 2016

## 1 Blind Algorithm - Random Walk

The first attempts to search for optimal values of the *utility* function within the group of enumerative algorithms, whose aim was to calculate the objective value in all possible points and then comparing the obtained value for the *minimum* or *maximum*.

In essence, this means generating a user-defined number of *random points* on the search space and define a function which then selects an individual with a minimum value. This algorithm has no other ties to the development of individuals towards global extreme that is found on the quality of previous values.

```
input : iterations: maximum number of iterations,  
        argbest: the best solution found  
        fitness0: initial setting to a large value  
output: argbest: the best solution foundfor  $i \leftarrow 0$  to iterations doarg = rand_irand_i is a random number between the defined interval */fitness = F_{cost}(arg)if  $fitness < fitness_0$  thenfitness_0 = fitnessarg_{best} = argendend
```

Algorithm 1: Blind Search

## 2 Local Search

The method is based on the *initial solution* under consideration (usually randomly generated), which generates a set of *neighbouring* solutions. In order to find the best solution among those neighbours, if the found one is better than the default solution, we take it as

new current best solution and we again generate neighbours to it and look amongst them for “improved” solutions. This procedure is repeated until we decide that between neighbouring solutions there are no longer any improving solutions.

Stochasticity of this procedure is just a random selection of initial solutions, the following optimisation algorithm used is strictly deterministic. The method of local search (*LS*) is a (stochastic) algorithm with the following parameters:

$$LS = (M, x_0, N, f)$$

where:

- $M$  is the solution space
- $x_0$  is the initial solution. If  $x_0$  is determined randomly, then the method is stochastic local search algorithm.
- $\sigma \subseteq M \cdot M$  is a binary relation on  $M$  defining neighbouring solutions.
- $N(x, \sigma) = \{y \in M \mid (y, x) \in \sigma\}$  is the set of solutions which are neighbour of  $x, x \in M$
- $f$  is the objective function, the optimum seeking  $f : M \rightarrow R$

The following pseudocode describes the local search process. Boolean variable  $\tau$  serves as the termination criterion, which is **true** if a better solution is found in the neighborhood and **false** otherwise.  $x_0$  is the initial (pseudo-random) solution.

```

input :  $x_0$ : initial random solution
          $x^*$ : best solution found
          $\tau$ : boolean variable
output:  $x^*$ : best solution found
1  $x^* = x$           /* initialize best solution to the random solution */
2  $\tau = \text{true}$     /* initialize  $\tau$  to true */
4 while  $\tau = \text{true}$  do
5   |  $\tau = \text{false}$ 
6   | generate  $N(x^*, \sigma)$ 
7   | find  $x \in N(x^*, \sigma)$  so that  $f(x_{loc}) \leq f(x)$ , for each  $x \in N(x^*, \sigma)$ 
8   | if  $f(x) < f(x^*)$  then
9   |   |  $x^* = x_{loc}$ ;
10  |   |  $\tau = \text{true}$ ;
11  | end
12 end

```

**Algorithm 2:** Local Search

### 3 Iterative Local Search

There are several ways to reduce the likelihood of deadlock in a local optimum, namely:

- enlarge the set of neighbours.
- repeat the method of local search for several different (pseudo-randomly generated) initial solutions and record the best solution.
- to admit even steps, after which there is a deterioration in the value of objective function, thereby allowing the “turn” to another area of space solution.

All these methods offer hope of obtaining a better solution, but require longer calculation time. The second method, known as the repeated local search can be formally written as follows:

$$RLS = (M, x_0, N, f, t_{max})$$

where:

- $M$  is the solution space
- $x_0$  is the initial solution. If  $x_0$  is determined randomly, then the method is stochastic local search algorithm.
- $\sigma \subseteq M \cdot M$  is a binary relation on  $M$  defining neighbouring solutions.
- $N(x, \sigma) = \{y \in M | (y, x) \in \sigma\}$  is the set of solutions which are neighbour of  $x, x \in M$
- $f$  is the objective function, the optimum seeking  $f : M \rightarrow R$
- $t_{max}$  parameter specifies the chosen number of iterations the algorithm performs a local search and criteria for termination.

The following pseudocode describes the repeated local search process. Boolean variable  $\tau$  serves as the termination criterion, which is **true** if a better solution is found in the neighborhood and **false** otherwise.  $x_0$  is the initial (pseudo-random) solution, and  $t_{max}$  is the maximum number of iterations.

```

input :  $x_{0t}$ : initial random solution
          $x^*$ : best global solution
          $x_t^*$ : best global solution in each iteration
          $\tau$ : boolean variable
          $t_{max}$ : maximum number of iterations
output:  $x^*$ : best solution found

1  $x_t^* = x_{0t}$       /* initialize iterative best solution      */
2  $x^* = x_{0t}$       /* initialize global best solution      */
3  $\tau = \text{true}$    /* initialize  $\tau$  to true              */
4  $t = 1$            /* initialize  $t$  to 1                  */
6 while  $t \leq t_{max}$  do
8   while  $\tau = \text{true}$  do
9      $\tau = \text{false}$ 
10    generate  $N(x^*, \sigma)$ 
11    find  $x \in N(x^*, \sigma)$  so that  $f(x_{loc}) \leq f(x)$ , for each  $x \in N(x^*, \sigma)$ 
12    if  $f(x_{loc}) < f(x_t^*)$  then
13       $x_t^* = x_{loc}$ ;
14       $\tau = \text{true}$ ;
15    end
16  end
17  if  $f(x^*) < f(x_t^*)$  then
18     $x^* = x_t^*$ ;
19    /* update the best solution after  $t$  interactions      */
20  end
21   $t = t + 1$     /* update the  $t$  counter              */
22   $x_t^* = x_{0t}$  /* (randomly) choose a new initial solution  $x_{0t}$       */
23 end

```

**Algorithm 3:** Repeated Local Search

## 4 Experimentation

The student is required to modify the code from Lab 1 and add the three described algorithms. For each algorithm, 30 iterations for each problem is required for 10, 20 and 30 dimensions. Compute statistical analysis on the obtained results for average, standard deviation, range, median and time.

## Submission

The student must submit the following separate files to canvas:

1. source codes for the problems
2. a L<sup>A</sup>T<sub>E</sub>X typeset report on the results and its analysis

The report must contain an introduction in the algorithms, the full experimentation results in tabular format and condensed results with statistical analysis compared with what was obtained in Lab 1.

The files must be submitted through Canvas by midnight October 24, 2016. The penalty for late submission is 10% for 1 day, 20% for 2 day, after which it will be zero. The grading rubric is given in Table 1.

Table 1: Grading rubric

File	Aspects	Points
Code	Compiles and executes	35
	Explanation	15
Report	Results	25
	Analysis	25